## Systematic Detection of Highways of Horizontal Gene Transfer

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## What is Horizontal Gene Transfer?

Basic Problem: Infer the HGT events in the evolutionary history of a given set of species.


## Inferring HGTs

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HGT Inference Problem: Find the fewest HGT edges on a given species tree to explain a given gene tree. This problem is NP-hard [Hallett and Lagergren (2001), Bordewich and Semple (2005)].

## Highways of HGT

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Inferring highways is important for understanding evolution of prokaryotes.

## The Highway Problem

The Highway Problem: Given a set of (rooted or unrooted) gene trees $\mathcal{G}$ and the corresponding (rooted) species tree $S$, infer the highways of gene transfer on $S$.

Gene Trees


## Existing Approach for the Highway Problem

## Existing approach:

- Considers each gene tree one at a time.
- Heuristically infers the HGT edges on the species tree, for that gene tree.
- Combines these individual solutions to paint an overall picture.
- Solving the HGT inference problem is NP-hard
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Our approach tackles the highway problem directly and avoids these pitfalls.

## Our Approach for the Highway Problem

- Decompose each gene tree into its constituent set of quartet trees.
- Combine all the quartet trees into a single weighted set.
- Identify the quartet trees that are inconsistent with given species tree.
- Horizontal edges that can explain the most (normalized) inconsistent quartets are the proposed highways.


## Our Approach for the Highway Problem

Based on quartets.
A quartet is a set of four species. Given a tree, each quartet, say $\{A, B, C, D\}$, induces one of these three topologies in the tree.


## Our Approach for the Highway Problem

For example, given $S$ and quartet $\{A, C, F, G\}$.


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## Main Computational Problem

Highway scoring problem: Given a weighted set of inconsistent quartet trees and a rooted species tree on $n$ taxa, find the (raw) score of every horizontal edge.

The (raw) score of any horizontal edge is the total weight of all inconsistent cuartet trees that can he exnlained by an HGT event along that horizontal edge.

Can be solved naively in $O\left(n^{6}\right)$ time: Evaluate each of the $O\left(n^{2}\right)$ horizontal edges on the $O\left(n^{4}\right)$ auartet trees We developed an algorithm that computes all scores in $O\left(n^{4}\right.$

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- Can be solved naïvely in $O\left(n^{6}\right)$ time: Evaluate each of the $O\left(n^{2}\right)$ horizontal edges, on the $O\left(n^{4}\right)$ quartet trees.
- We developed an algorithm that computes all scores in $O\left(n^{4}\right)$ time. This is optimal.


## Crucial Structural property

## Species tree



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1. Move $G$ towards $A$.
2. Move $A$ towards $G$.
3. Move $C$ towards $F$.
4. Move $F$ towards $C$.

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4. Move $F$ towards $C \Rightarrow\langle d, e \rightarrow F\rangle$.

Depending on how the quartet is embedded in the species tree, we can always get something similar.

## Our Algorithm

We make use of this characterization to decorate the species tree with the subtree-path pairs for all the quartet trees.

We then use a dynamic programming algorithm to compute the score of each horizontal edge.

## Our Algorithm

- Decorating the species tree, for each quartet tree, takes $O(1)$ time.
- The dynamic programming algorithm takes $O\left(n^{2}\right)+$ $O$ (Number of quartet trees) time.
- Total time Complexity: $=O\left(n^{2}\right)+O$ (Number of quartet trees), i.e., $O\left(n^{4}\right)$.


## Normalization

Different HGTs can explain different numbers of inconsistent quartets. Normalization of edge scores: Divide raw score of a horizontal edge
by the maximum number of inconsistent quartets that could be
explained by an HGT event along that edge. We developed an $O\left(n^{2}\right)$-time algorithm to normalize all the raw cores.

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## Simulation Study

Measure the effect of noise on highway inference:

- Simulated data sets of 50 taxa, 1000 gene trees.
- Randomly implanted highway affecting $10 \%$ of genes.
- Noise levels: 0, 500, 1000, 1500, 2000, and 2500 HGTs, with each HGT event affecting a gene chosen at random with replacement.
- 50 data sets for each noise level.


## Simulation Study



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## Simulation Study



## Running time

To analyze any dataset we:

1. Decompose the gene trees to generate the weighted set of quartets: $O\left(t \cdot n^{4}\right)$ time
2. Solve the highway scoring problem: $O\left(n^{4}\right)$ time

## The bottleneck is thus the quartet decomposition step

Still, we can quickly analyze fairly large datasets:
> 50 taxa, 1000 gene trees: 30 seconds,
$\rightarrow 100$ taxa, 1000 gene trees: 15 minutes,

- 200 taxa, 1000 gene trees: 5 hours


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## Shortcomings of This Approach

Two main shortcomings:

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E.g., Consider some highway $\left\{x_{1}, y_{1}\right\}$ that transfers 100 genes. Let $x_{1} \rightarrow y_{1}$ give 10 inconsistent quartets and $y_{1} \rightarrow x_{1}$ give 30 inconsistent quartets.
All transfers in $x_{1} \rightarrow y_{1}$ direction imply total normalized score of $10 \times 100 / N F$, while all if transfers are in the other direction then score is $30 \times 100 / N F$.

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All transfers in $x_{1} \rightarrow y_{1}$ direction imply total normalized score of $10 \times 100 / N F$, while all if transfers are in the other direction then score is $30 \times 100 / N F$.
2. If a gene tree has too many missing leaves, it cannot be used in the analysis.

## Our New Method

Same basic idea, but look at the quartet decomposition of each gene tree separately and normalize scores at gene tree level.

Addresses both the problems mentioned in previous slide, and improves performance drastically.

## Our New method

1: For each input gene tree $G_{i}$, for $1 \leq i \leq k$, 1(a): Decompose $G_{i}$ into its constituent set of quartet trees, denoted $\Phi_{i}$.
1(b): Remove from $\Phi_{i}$ all those quartet trees that are consistent with $S$ (or that can be explained by a previously inferred highway).
1(c): For each horizontal edge $\{u, v\} \in H(S)$, compute the normalized score $N S\left(\{u, v\}, \Phi_{i}\right)$.
2: For each horizontal edge $\{u, v\} \in H(S)$, compute its final score, denoted score $\{u, v\}$, to be $\sum_{i=1}^{k} N S\left(\{u, v\}, \Phi_{i}\right)$.
3: Select the highest scoring horizontal edge as a highway.

## Our New method

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So we compute normalized scores of the directed HGT events and assign $N S\left(\{u, v\}, \Phi_{i}\right)=\max \left\{N S\left((u, v), \Phi_{i}\right), N S\left((v, u), \Phi_{i}\right)\right\}$.

## Comparative Results

- Global-Normalization $\approx$ PG-Norm



## Comparative Results



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$$
\text { Global-Normalization } \diamond \text { PG-Norm } \nabla \text { PG-Norm-Exp(2) }
$$



## Comparative Results

- Global-Normalization $\Rightarrow$ PG-Norm $\nabla$ PG-Norm-Exp(2)


Bansal et al. Highways of HGT

## Comparative Results



## Time Complexity

Essentially the same as the previous method: $O\left(t \cdot n^{4}\right)$
Slower by approximately a constant factor of 16 .

## Biological Data Analysis

- Dataset of 144 prokaryotic species and over 22000 gene families.
- Each gene family represented by 100 gene trees.
- Each iteration takes less than 6 hours!


## Conclusion

Our new approach:

- Looks at combined data from all gene trees to detect fingerprints of highways.
- Bypasses need to infer individual HGT events.
- Highly accurate at even high rates of HGT or noise.
- Capable of efficiently handling even very large datasets.
- Can deal cleanly with uncertainty in gene trees.


## Thank You!

Questions!

